





This poli cy has been largely adapted from the White Rose Maths Calculation Policy with further material added. It is a working document and will be revised and amended as necessary.

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WESTON VILLAGE PRIMARY SCHOOL



THE EARLY YEARS FOUNDATION STAGE

Mathematics involves providing children with opportunities to develop and improve their skills in counting, understanding and using numbers, calculating simple addition and subtraction problems; and to describe shapes, spaces, and measures.

Maths for young children should be meaningful. Where possible, concepts should be taught in the context of real life.

(Statutory Framework for the Early Years Foundation Stage, DfE: 2012





EYFS Addition



representations.

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than ...?

GUIDANCE / MODELS AND IMAGES KEY VOCABULARY If available, Numicon shapes are introduced straight away and can be used to: Games and songs identify 1 more/less can be a useful way combine pieces to add. to begin using find number bonds. vocabulary involved add without counting. in addition e.g. Children can record this by printing or drawing around Numicon Alice the Camel pieces. Children begin to combine groups of objects using concrete apparatus add more Construct number sentences verbally or using cards to go with practical activities. and make Children are encouraged to read number sentences aloud in different ways "Three add two equals 5" "5 is equal to three and two" sum total Children make a record in pictures, words or symbols of addition activities already carried out. altogether Solve simple problems using fingers score double 2 3 5 Number tracks can be introduced to count up on and to find one more: one more, two more, ten more What is 1 more than 4? 1 more than 13? how many more to Number lines can then be used alongside number tracks and practical apparatus to make...? solve addition calculations and word problems. how many more is... Children will need opportunities to look at and talk about different models and images as they move between





EYFS - Subtraction

GUIDANCE / MODELS AND IMAGES		KEY VOCABULARY
Children begin with mostly pictorial representations XXX XX		Games and songs can be a useful way to begin using vocabulary involved in subtraction
Concrete apparatus is used to relate subtraction to taking away and counting how many	X	e.g. Five little men in a flying
objects are left.	5 - 1 = 4	saucer
Concrete apparatus models the subtraction of 2 objects from a set of 5.		W. DOWNERS
Construct number sentences verbally or using cards to go with practical activities.		take (away)
Children are encouraged to read number sentences aloud in different ways "five subtract one I	eaves four" "four is	leave
equal to five subtract one"		how many are left/left
		over?
Children make a record in pictures, words or symbols of subtraction activities already carried o	ut.	ASSESSMENT AND ADDRESS OF THE PARTY OF THE P
		how many have gone?
Solve simple problems using fingers		one less, two less ten
		less
Number tracks can be introduced to count back and to find one less:		
Number tracks can be introduced to count back and to find one less:		how many fewer is
What is 1 less than 9? 1 less than 20?		than?
M. DECORPTION OF THE PROPERTY	5442 - 25250 J. 155	difference between
Number lines can then be used alongside number tracks and practical	45678910	is the same as
apparatus to solve subtraction calculations and word problems. Children 9 1 2 3 count back under the number line.	A Charles	is the same as
event been street the frombet time.	- lab	
Children will need opportunities to look at and talk about different models and images as the representations.	y move between	





EYFS - Multiplication

GUIDANCE / MOI	DELS AND IMAGES	KEY VOCABULARY
The link between addition and multiplication can be intro	duced through doubling.	lots of
favailable, Numicon is used to visualise the repeated add	ding of the same number.	Tarte Care Care Care Care Care Care Care Car
These can then be drawn around or printed as a way of re		groups of
1823		times
Children begin with mostly pictorial representations:		multiply
\bigcirc		multiplied by
(xx) (xx) (xx)		multiple of
How many groups of 2 are there?		
		once, twice, three
Real life contexts and use of practical equipment to count	t in repeated groups of the same size:	times ten times
CALL CALL CONTRACTOR		times as (big, long, wide and so on)
How many wheels are there altogether?	How much money do I have?	
		repeated addition
Count in twos; fives; tens both aloud and with	objects	double
Children are given multiplication problems set in a real life	a contact. Children are ancouraged to visualise the	
problem.	<u>contest</u> . Similar are encouraged to visualise the	
How many fingers on two hands? How many sides on th	ree triangles? How many legs on four ducks?	
Children are encouraged to read number sentences aloud to five multiplied by two"	d in different ways "five times two makes ten" "ten is equal	



WESTON VILLAGE PRIMARY SCHOOL



GUIDANCE / MODELS AND IMAGES	KEY VOCABULARY
The ELG states that children solve problems, including doubling, halving and sharing.	halve
Children need to see and hear representations of division as both grouping and sharing.	share, share equally
Division can be introduced through halving.	one each, two each, three each
Children begin with mostly pictorial representations linked to real life contexts:	group in pairs, threes
Grouping model	tens
X X Mum has 6 socks. She grouped them into pairs – how many pairs did she	equal groups of
make?	divide
Sharing model	divided by
I have 10 sweets. I want to share them with my friend. How many will we have each?	divided into
	left, left over
Children have a go at recording the calculation that has been carried out.	

FRACTIONS

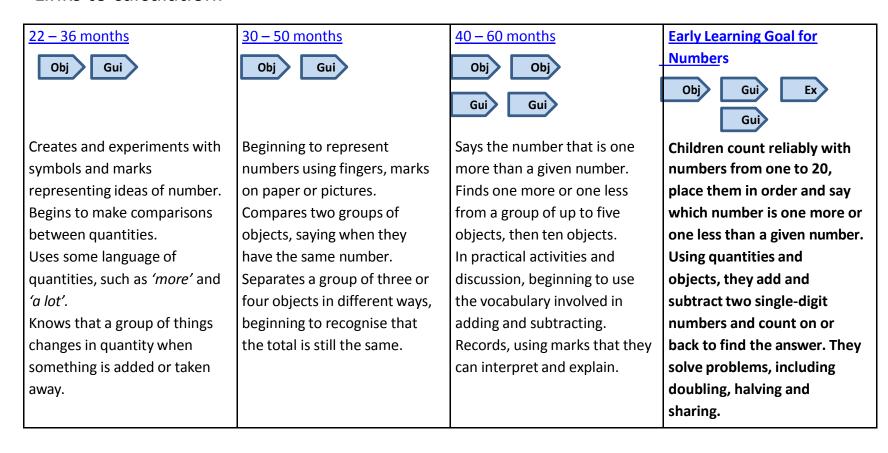
GUIDANCE / MODELS AND IMAGES	KEY VOCABULARY
Although not explicit in the Development Matters document, the sharing model is a useful way of introducing young	As division vocabulary
children to fractions and calculating with fractions.	plus:
	fraction
Setting the problems in real life context and solving them with <u>concrete apparatus</u> will support children's understanding.	half
and crading.	halves
"I have got 5 bones to share between my two dogs. How many bones will they get each?"	third
Children have a go at recording the calculation that has been carried out.	thirds

Development Matters in the Early Years Foundation Stage (EYFS)

This non-statutory guidance material supports practitioners in implementing the statutory requirements of the EYFS.

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Links to calculation:



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	A Unique Child: observing what a child is learning	Positive Relationships: what adults could do	Enabling Environments: what adults could provide
Birth - 11 months	Notices changes in number of objects/images or sounds in group of up to 3.	Sing number rhymes as you dress or change babies, e.g. 'One, Two, Buckle My Shoe'. Move with babies to the rhythm patterns in familiar songs and rhymes. Encourage babies to join in tapping and clapping along to simple rhythms.	Display favourite things so that a young baby can see them. Provide a small group of the same objects in treasure baskets, as well as single items, e.g. two fir cones or three shells. Create a mobile, occasionally changing the number of items you hang on it. Collect number rhymes which are repetitive and are related to children's actions and experiences, for
3-20 months	 Develops an awareness of number names through their enjoyment of action rhymes and songs that relate to their experience of numbers. Has some understanding that things exist, even when out of sight. 		example, 'Peter Hammers with One Hammer'. • Use song and rhymes during personal routines, e.g. 'Two Little Eyes to Look Around', pointing to their eyes, one by one. • Collect number and counting rhymes from a range of cultures and in other languages. This will benefit all children and will give additional support for children learning English as an additional language.
5-26 months	Knows that things exist, even when out of sight. Beginning to organise and categorise objects, e.g. putting all the teddy bears together or teddies and cars in separate piles. Says some counting words randomly.	Use number words in meaningful contexts, e.g. 'Here is your other mitten. Now we have two'. Talk to young children about 'lots' and 'few' as they play. Talk about young children's choices and, where appropriate, demonstrate how counting helps us to find out how many. Talk about the maths in everyday situations, e.g. doing up a coat, one hole for each button. Tell parents about all the ways children learn about numbers in your setting. Have interpreter support or translated materials to support children and families learning English as an additional language	Provide varied opportunities to explore 'lots' and 'few' in play. Equip the role-play area with things that can be sorted in different ways. Provide collections of objects that can be sorted and matched in various ways. Provide resources that support children in making one-to-one correspondences, e.g. giving each dolly a cup.
2-36 months	Selects a small number of objects from a group when asked, for example, 'please give me one', 'please give me two'. Recites some number names in sequence. Creates and experiments with symbols and marks representing ideas of number. Begins to make comparisons between quantities. Uses some language of quantities, such as 'more' and 'a lot'. Knows that a group of things changes in quantity when something is added or taken away.	Encourage parents of children learning English as an additional language to talk in their home language about quantities and numbers. Sing counting songs and rhymes which help to develop children's understanding of number, such as 'Two Little Dickie Birds'. Play games which relate to number order, addition and subtraction, such as hopscotch and skittles and target games.	Make a display with the children about their favourite things. Talk about how many like apples, or which of them watches a particular TV programme at home. Provide props for children to act out counting songs and rhymes. Provide games and equipment that offer opportunities for counting, such as skittles. Plan to incorporate a mathematical component in areas such as the sand, water or other play areas.

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	Mathematics: Numbers			
	A Unique Child: observing what a child is learning	Positive Relationships: what adults could do	Enabling Environments: what adults could provide	
30-50 months	Uses some number names and number language spontaneously. Uses some number names accurately in play. Recites numbers in order to 10. Knows that numbers identify how many objects are in a set. Beginning to represent numbers using fingers, marks on paper or pictures. Sometimes matches numeral and quantity correctly. Shows curiosity about numbers by offering comments or asking questions. Compares two groups of objects, saying when they have the same number. Shows an interest in number problems. Separates a group of three or four objects in different ways, beginning to recognise that the total is still the same. Shows an interest in numerals in the environment. Shows an interest in representing numbers. Realises not only objects, but anything can be counted, including steps, claps or jumps.	Use number language, e.g. 'one', 'two', 'three', 'lots', 'fewer', 'hundreds', 'how many?' and 'count' in a variety of situations. Support children's developing understanding of abstraction by counting things that are not objects, such as hops, jumps, dicks or claps. Model counting of objects in a random layout, showing the result is always the same as long as each object is only counted once. Model and encourage use of mathematical language e.g. asking questions such as 'How many saucepans will fit on the shelf?' Help children to understand that one thing can be shared by number of pieces, e.g. a pizza. As you read number stories or rhymes, ask e.g. 'When one more frog jumps in, how many will there be in the pool altogether?' Use pictures and objects to illustrate counting songs, rhymes and number stories. Encourage children to use mark-making to support their thinking about numbers and simple problems. Talk with children about the strategies they are using, e.g. to work out a solution to a simple problem by using fingers or counting aloud.	Give children a reason to count, e.g. by asking them to select enough wrist bands for three friends to play with the puppets. Enable children to note the 'missing set', e.g. 'There are none left' when sharing things out. Provide number labels for children to use, e.g. by putting a number label on each bike and a corresponding number on each parking space. Include counting money and change in role-play games. Create opportunities for children to separate objects into unequal groups as well as equal groups. Provide story props that children can use in their play, e.g. varieties of fruit and several baskets like Handa's in the story Handa's Surprise by Elleen Browne.	
40-60+ months	Recognises numerals of personal significance. Recognises numerals 1 to 5. Counts up to three or four objects by saying one number name for each item. Counts actions or objects which cannot be moved. Counts objects to 10, and beginning to count beyond 10. Counts out up to six objects from a larger group.	Encourage estimation, e.g. estimate how many sandwiches to make for the pionic. Encourage use of mathematical language, e.g. number names to ten: 'Have you got enough to give me three?' Ensure that children are involved in making displays, e.g. making their own pictograms of lunch choices. Develop this as a 3D representation using bricks and discuss the most popular choices. Add numerals to all areas of learning and development, e.g. to a display of a favourite story, such as 'The Three Billy Goats Gruff'.	Provide collections of interesting things for children to sort, order, count and label in their play. Display numerals in purposeful contexts, e.g. a sign showing how many children can play on a number track. Use tactile numeral cards made from sandpaper, velve or string. Create opportunities for children to experiment with a number of objects, the written numeral and the written number word. Develop this through matching activities with a range of numbers, numerals and a selection of objects.	

Development Matters in the Early Years Foundation Stage (EYFS)

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A Unique Child:	Positive Relationships:	Enabling Environments:
observing what a child is learning	what adults could do	what adults could provide
Selects the correct numeral to represent 1 to 5, then 1 to 10 objects. Counts an irregular arrangement of up to ten objects. Estimates how many objects they can see and checks by counting them. Uses the language of 'more' and 'fewer' to compare two sets of objects. Finds the total number of items in two groups by counting all of them. Says the number that is one more than a given number. Finds one more or one less from a group of up to five objects, then ten objects. In practical activities and discussion, beginning to use the vocabulary involved in adding and subtracting. Records, using marks that they can interpret and explain. Begins to identify own mathematical problems based on own interests and fascinations. Early Learning Goal Children count reliably with numbers from one to 20, place them in order and say which number is one more or one less than a given number. Using quantities and objects, they add and subtract two single-digit numbers and count on or back to find the answer. They solve problems, including doubling, halving and sharing.	Make books about numbers that have meaning for the child such as favourite numbers, birth dates or telephone numbers. Use rhymes, songs and stories involving counting on and counting back in ones, twos, fives and tens. Emphasise the empty set and introduce the concept of nothing or zero. Show interest in how children solve problems and value their different solutions. Make sure children are secure about the order of numbers before asking what comes after or before each number. Discuss with children how problems relate to others they have met, and their different solutions. Talk about the methods children use to answer a problem they have posed, e.g. 'Get one more, and then we will both have two.' Encourage children to make up their own story problems for other children to solve. Encourage children to extend problems, e.g. "Suppose there were three people to share the bricks between instead of two". Use mathematical vocabulary and demonstrate methods of recording, using standard notation where appropriate. Give children learning English as additional language opportunities to work in their home language to ensure accurate understanding of concepts.	Use a 100 square to show number patterns. Encourage children to count the things they see and talk about and use numbers beyond ten Make number games readily available and teach children how to use them. Display interesting books about number. Play games such as hide and seek that involve counting. Encourage children to record what they have done, e.g. by drawing or tallying. Use number staircases to show a starting point and how you arrive at another point when something is added or taken away. Provide a wide range of number resources and encourage children to be creative in identifying and devising problems and solutions in all areas of learning. Make number lines available for reference and encourage children to use them in their own play. Big number lines may be more appropriate than counters for children with physical impairments. Help children to understand that five fingers on each hand make a total of ten fingers altogether, or that two rows of three eggs in the box make six eggs altogether.

Additional information for the 'exceeding' judgement

Taken from the 2014 Early Years Foundation Stage Handbook

Numbers: Children estimate a number of objects and check quantities by counting up to 20. They solve practical problems that involve combining groups of 2, 5, or 10, or sharing into equal groups.

(This descriptor has been amended to reflect the increased level of challenge applied to the expected descriptor following the Tickell review.)

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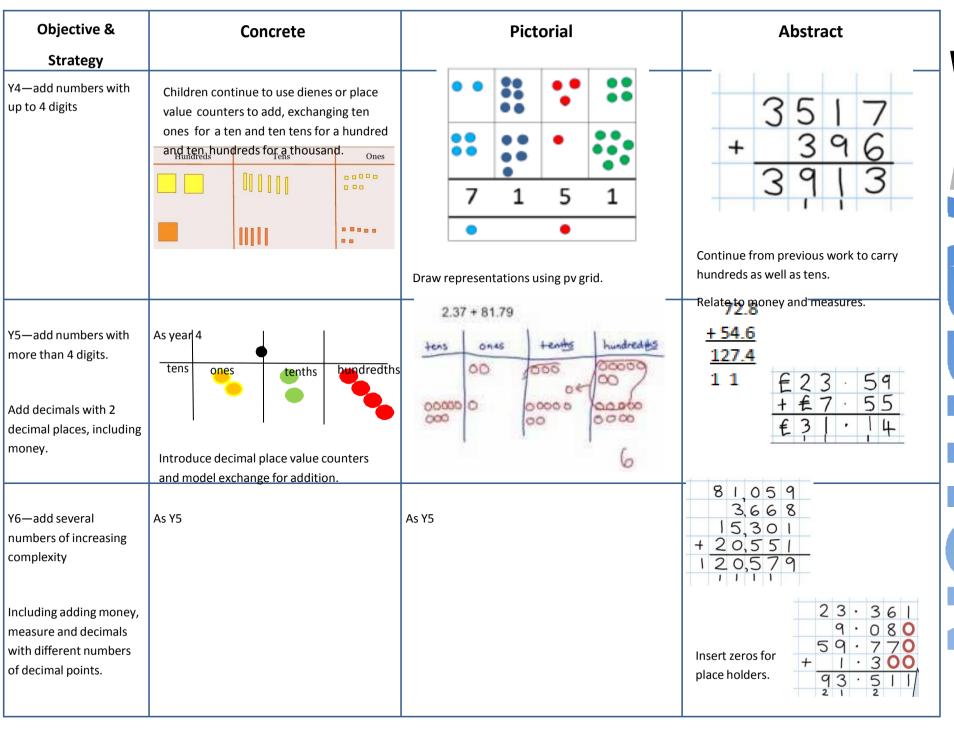
Objective & Strategy	Concrete	Pictorial	Abstract
Combining two parts to make a whole: part- whole model	Use part part whole model. Use cubes to add two numbers together as a group or in a bar.	Use pictures to add two numbers together as a group or in a bar.	4 + 3 = 7 Use the part-part whole diagram as shown above to move into the abstract.
Starting at the big- ger number and counting on	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	12 + 5 = 17 Start at the larger number on the number line and count on in ones or in one jump to find the answer.	5 + 12 = 17 Place the larger number in your head and count on the smaller number to find your answer.
Regrouping to make 10. This is an essential skill for column addition later.	Start with the bigger number and use the smaller number to make 10. Use ten frames.	Use pictures or a number line. Regroup or partition the smaller number using the part part whole model to make 10. 9 + 5 = 14 1 4 1 4 1 4 1 4 1 4 1 4 1 4	7 + 4= 11 If I am at seven, how many more do I need to make 10. How many more do I add on now?
Represent & use number bonds and related subtraction facts within 20	2 more than 5.	Draw 2 more hats 5 + 2 =	Emphasis should be on the language '1 more than 5 is equal to 6.' '2 more than 5 is 7.' '8 is 3 more than 5.'

Objective &	Concrete	Pictorial	Abstract	
Strategy				
Adding multiples of	50= 30 = 20		20 + 30 = 50	
ten	11111		70 = 50 + 20	
		3 tens + 5 tens = tens 30 + 50 =	40 + □ = 60	
	Model using dienes and bead strings	Use representations for base ten.		
Use known number facts	Children explore ways of making numbers within 20	20	1 + 1 = 16	
		+= 20		
Using known facts		∵ + ⊹ = ∴	3 + 4 = 7	
		+ =	leads to	
		+ = = =	30 + 40 = 70 leads to	
		Children draw representations of H,T and O	300 + 400 = 700	
Bar model		看着看着看着 看 看 產	23 25	
			?	
	3 + 4 = 7	7 + 3 = 10	23 + 25 = 48	

Objective &	Concrete	Pictorial	Abstract
Strategy			
Add a two digit number and ones	Use ten frame to make 'magic ten Children explore the pattern. 17 + 5 = 22 27 + 5 = 32	Use part part whole and number line to model. 17 + 5 = 22 20 16 + 7	17 + 5 = 22 Explore related facts 17 + 5 = 22 5 + 17 = 22 22
Add a 2 digit num- ber and tens	25 + 10 = 35 Explore that the ones digit does not change	27 + 30 +10 +10 +10 	27 + 10 = 37 27 + 20 = 47 27 + = = 57
Add two 2-digit numbers	Model using dienes , place value counters and numicon	+20 +5 Or +20 +3 +2 47 67 72 47 67 70 72 Use number line and bridge ten using part whole if necessary.	25 + 47 20 + 5 40 + 7 20 + 40 = 60 5+ 7 = 12 60 + 12 = 72
Add three 1-digit numbers	Combine to make 10 first if possible, or bridge 10 then add third digit	Regroup and draw representation. + = 15	4+7+6 = 10+7 = 17 Combine the two numbers that make/ bridge ten then add on the third.

		I	T T
Objective &	Concrete	Pictorial	Abstract
Strategy			
Column Addition—no regrouping (friendly numbers)	T O Model using Dienes or numicon Add together the ones first, then the	Children move to drawing the counters using a tens and one frame.	2 2 3
Add two or three 2 or 3-digit numbers.	tens. Tens Units 45 34 7 9 Calculations 21 + 42 = 21 + 42 = 21 + 42 = And the property of the propert	tens ones	+ 1 1 4 3 3 7 Add the ones first, then the tens, then the hundreds.
Column Addition with regrouping.	Exchange ten ones for a ten. Model using numicon and pv counters. 146 + 527	Children can draw a representation of the grid to further support their understanding, carrying the ten underneath the line	$\begin{array}{cccccccccccccccccccccccccccccccccccc$





Objective & Strategy	Concrete	Pictorial	Abstract
Taking away ones.	Use physical objects, counters, cubes etc. to show how objects can be taken away. $6-4=2$		7—4 = 3
	4-2=2	$15 - 3 = \boxed{12}$ Cross out drawn objects to show what has been taken away.	16—9 = 7
Counting back	Move objects away from the group, counting backwards. Move the beads along the bead string as you count backwards.	5 - 3 = 2 Count back in ones using a number line.	Real life worded problems e.g. Put 13 in your head, count back 4. What number are you at?
Find the Difference	Compare objects and amounts 7 'Seven is 3 more than four' 4 'I am 2 years older than my sister' 5 Pencils Lay objects to represent bar model.	Count on using a number line to find the difference. +6 1 2 3 4 5 6 7 8 9 10 11 12	Real life worded problems e.g. Hannah has 12 sweets and her sister has 5. How many more does Hannah have than her sister?

Objective &	Concrete	Pictorial	Abstract
Strategy			
Represent and use number bonds and related subtraction facts within 20 Part Whole model	Link to addition. Use PPW model to model the inverse. If 10 is the whole and 6 is one of the arts, what s the other part?		Move to using numbers within the part whole model. 5 12 7
	10—6 = 4	Use pictorial representations to show the part.	
Make 10		13 - 7 = 6 -43 - 7	16—8 How many do we take off first to get to 10? How many left to take off?
	Make 14 on the ten frame. Take 4 away to make ten, then take one more away so	Jump back 3 first, then another 4. Use ten as the stopping point.	
Bar model	that you have taken 5.	*****	8 2
	5—2 = 3		10 = 8 + 2
	J Z - J		10 = 2 + 8
			10—2 = 8
			10—8 = 2

Objective & Strategy	Concrete	Pictorial	Abstract
Regroup a ten into ten ones	Use a PV chart to show how to change a ten into ten ones, use the term 'take and make'	20 – 4 =	20—4 = 16
Partitioning to sub- tract without re- grouping. 'Friendly numbers'	Use Dienes to show how to partition the number when subtracting without regrouping.	Children draw representations of Dienes and cross off. 43—21 = 22	43—21 = 22
Make ten strategy Progression should be crossing one ten, crossing more than one ten, crossing the hundreds.	34—28 Use a bead bar or bead strings to model counting to next ten and the rest.	76 80 90 93 'counting on' to find 'difference' Use a number line to count on to next ten and then the rest.	93—76 = 17

Objective & Strategy	Concrete	Pictorial	Abstract
Column subtraction without regrouping (friendly numbers)	Use base 10 or Numicon to model	Darw representations to support understanding	$47 - 24 = 23$ $-\frac{40 + 7}{20 + 3}$ Intermediate step may be needed to lead to clear subtraction understanding. 32 -12 20
Column subtraction with regrouping	Begin with base 10 or Numicon. Move to pv counters, modelling the exchange of a ten into tten ones. Use the phrase 'take and make' for exchange.	Tens lones Tens l	836-254=582 Begin by partitioning into pv columns $728-582=146$ Then move to formal method.

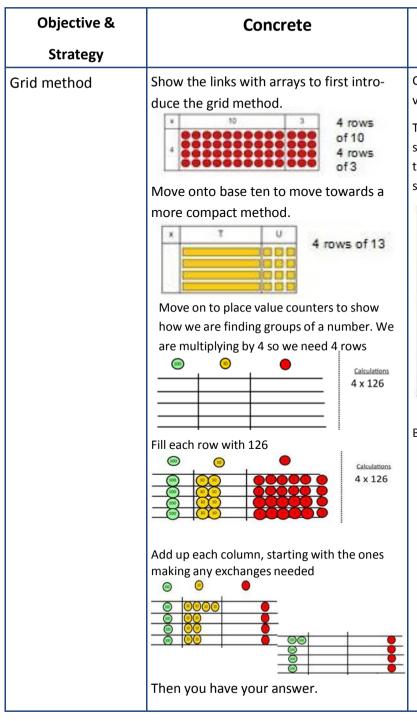
Objective &	Concrete	Pictorial	Abstract
Strategy Subtracting tens	234 - 179	Children to draw pv counters and show their	
and ones Year 4 subtract with up to 4 digits. Introduce decimal subtraction through context of money	Model process of exchange using base ten and then move to PV counters.	exchange—see Y3	2 7 5 4 - 1 5 6 2 1 1 9 2 Use the phrase 'take and make' for exchange
Year 5- Subtract with at least 4 digits, including money and measures. Subtract with decimal values, including mixtures of integers and decimals and aligning the decimal	As Year 4	Children to draw place value counters and show their exchange—see Y3	13 10 3 6 6 6 6 6 6 6 6 6
Year 6—Subtract with increasingly large and more complex numbers and decimal values.			"X" 8 10, 6 9 9 - 89, 9 4 9 60, 7 5 0 "Y 10 '5 · 34 '1 9 kg - 36 · 08 0 kg 69 · 33 9 kg

Objective &	Concrete	Pictorial	Abstract
Strategy Doubling	Use practical activities using manipultives including cubes and Numicon to demonstrate doubling	Draw pictures to show how to double numbers	Partition a number and then double each part before recombining it back together.
	double 4 is 8 4 × 2 = 8	Double 4 is 8	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
Counting in multiples	Count the groups as children are skip counting, children may use their fingers as they are skip counting.	Children make representations to show counting in multiples.	Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30
Making equal groups and counting the total	x = 8 Use manipulatives to create equal groups.	Draw to show 2 x 3 = 6 Draw and make representations	2 x 4 = 8

Objective &	Concrete	Pictorial	Abstract
Strategy Repeated addition	Use different objects to add equal groups	Use pictorials including number lines to solve problems e.g. There are 3 sweets in one bag. How many sweets are in 5 bags altogether? 3+3+3+3+3 = 15	Write addition sentences to describe objects and pictures. 2+2+2+2 = 10
Understanding arrays	Use objects laid out in arrays to find the answers to 2 lots 5, 3 lots of 2 etc.	Draw representations of arrays to show understanding	3 x 2 = 6 2 x 5 = 10

Objective & Strategy	Concrete	Pictorial	Abstract
Doubling	Model doubling using dienes and PV counters. 40 + 12 = 52	Draw pictures and representations to show how to double numbers	Partition a number and then double each part before recombining it back together. $ \begin{array}{cccccccccccccccccccccccccccccccccc$
Counting in multiples of 2, 3, 4, 5, 10 from 0 (repeated addition)	Count the groups as children are skip counting, children may use their fingers as they are skip counting. Use bar models. 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 40	Number lines, counting sticks and bar models should be used to show representation of counting in multiples. 3 3 3 3 3	Count in multiples of a number aloud. Write sequences with multiples of numbers. 0, 2, 4, 6, 8, 10 0, 3, 6, 9, 12, 15 0, 5, 10, 15, 20, 25, 30

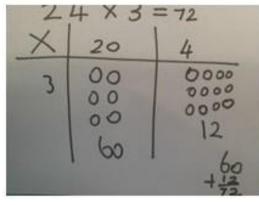
Objective & Strategy	Concrete	Pictorial	Abstract
Multiplication is commutative	Create arrays using counters and cubes and Numicon. Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.	Use representations of arrays to show different calculations and explore commutativity.	$12 = 3 \times 4$ $12 = 4 \times 3$ Use an array to write multiplication sentences and reinforce repeated addition. 00000 00000 $5 + 5 + 5 = 15$ $3 + 3 + 3 + 3 + 3 = 15$ $5 \times 3 = 15$ $3 \times 5 = 15$
Using the Inverse This should be taught alongside division, so pupils learn how they work alongside each other.		X	$2 \times 4 = 8$ $4 \times 2 = 8$ $8 \div 2 = 4$ $8 \div 4 = 2$ $8 = 2 \times 4$ $8 = 4 \times 2$ $2 = 8 \div 4$ $4 = 8 \div 2$ Show all 8 related fact family sentence



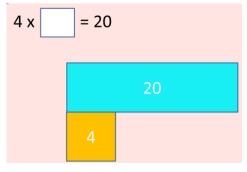
Pictorial

Children can represent their work with place value counters in a way that they understand.

They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below.



Bar model are used to explore missing numbers



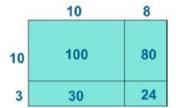
Abstract

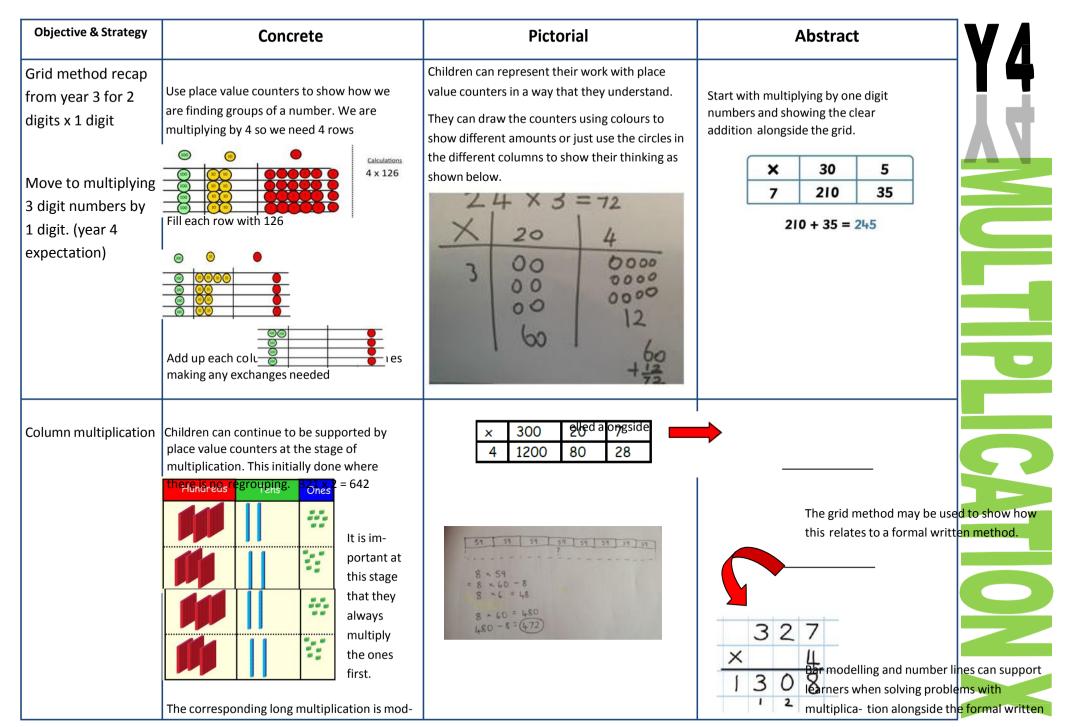
Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

×	30	5
7	210	35

$$210 + 35 = 245$$

Moving forward, multiply by a 2 digit number showing the different rows within the grid method.





methods.

327

x 4

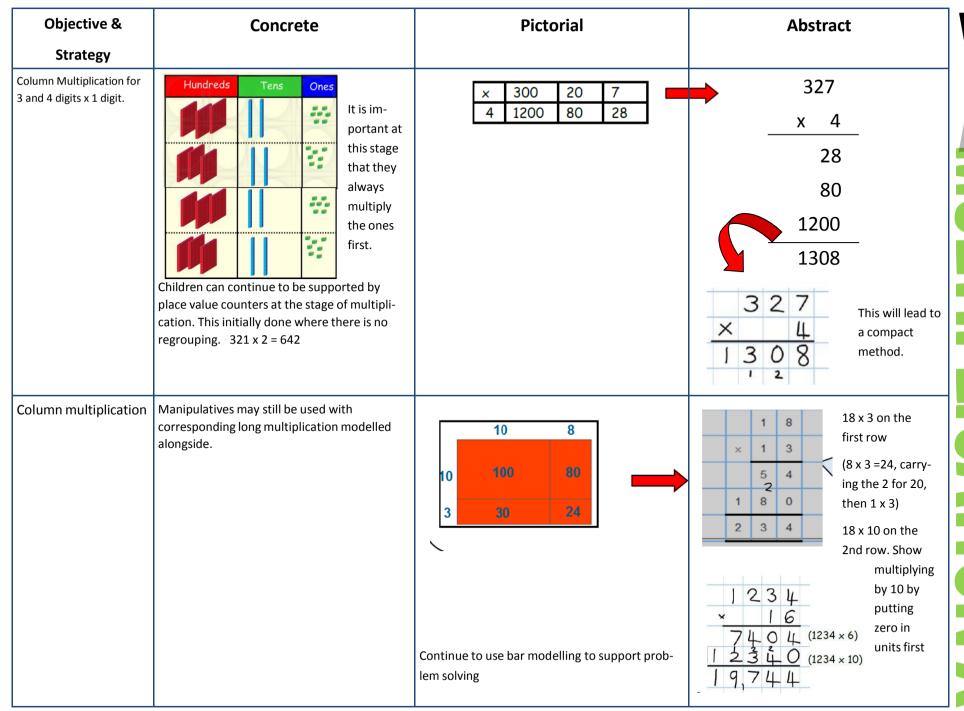
28

80

1200

1308

This may lead to a compact method.



Objective &	Concrete	Pictorial	Abstract
Multiplying decimals up to 2 decimal places by a single digit.			Remind children that the single digit belongs in the units column. Line up the decimal points in the question and the answer.
			3 · 1 9 × 8 2 5 · 5 2

Objective &	Concrete	Pictorial	Abstract
ivision as sharing		Children use pictures or shapes to share quantities. 8 shared between 2 is 4	12 shared between 3 is 4
	10	12 shared between 3 is 4	
	nave 10 cubes, can you share them equally in groups?		

Objective & Strategy	Concrete	Pictorial	Abstract
Division as sharing	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities. $8 \div 2 = 4$ Children use bar modelling to show and support understanding. 12 $12 \div 4 = 3$	12 ÷ 3 = 4
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.	Use number lines for grouping $ \begin{array}{cccccccccccccccccccccccccccccccccc$	28 ÷ 7 = 4 Divide 28 into 7 groups. How many are in each group?

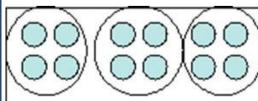
Objective &	Concrete	Pictorial	Abstract
Strategy			
Division as grouping	Use cubes, counters, objects or place value counters to aid understanding. 24 divided into groups of $6 = 4$ 96 ÷ 3 = 32	Continue to use bar modelling to aid solving division problems. $ \begin{array}{c} 20 \\ ? \\ \hline 20 \div 5 = ? \\ 5 \times ? = 20 \end{array} $	How many groups of 6 in 24? 24 ÷ 6 = 4
Division with arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$	Draw an array and use lines to split the array into groups to make multiplication and division sentences	Find the inverse of multiplication and division sentences by creating eight linking number sentences. 7 x 4 = 28 4 x 7 = 28 28 ÷ 7 = 4 28 ÷ 4 = 7 28 = 7 x 4 28 = 4 x 7 4 = 28 ÷ 7 7 = 28 ÷ 4

Objective &	Concrete	Pictorial	Abstract
Strategy			
Division with remainders.	Divide objects between groups and see how much is left over Example without 40 ÷ 5 Ask "How many Example with re 38 ÷ 6 For larger numbe jumps can be recommended.	5s in 40?" 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 8 f 0 5 10 15 20 25 30 35 40 mainder.	a remainder of 2

Objective &	Concrete		
Strategy			
Divide at least 3 digit	96 ÷ 3	Tens	Units
numbers by 1 digit.		3	2
Short Division		10 10 10	• •
SHOLL DIVISION	3	10 00 10	0 0
	Use place v		divide using the
		ethod alongside	
		9909	Calculations 42 ÷ 3
	-		
	42 ÷ 3=		1
	Start with the biggest place value, we are sharing 40 into three groups. We can put 1		
			ave 1 ten left over.
		10	
		10	
		100	
	-	10	
		ige this ten for te ones equally amo	en ones and then
	17	and Equally arrive	Mig the groups.
	We look ho	w much in 1 gro	oup so the answer
	is 14.		and the tributer

Pictorial

Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.



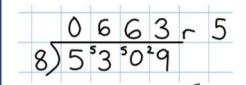
Encourage them to move towards counting in multiples to divide more efficiently.

Abstract

Begin with divisions that divide equally with no remainder.

Move onto divisions with a remainder.

Finally move into decimal places to divide the total accurately.





Step 1—a remainder in the ones

- 4 does not go into 1 (hundred). So combine the 1 hundred with the 6 tens (160).
- 4 goes into 16 four times.
- 4 goes into 5 once, leaving a remainder of 1.

- 8 does not go into 3 of the thousands. So combine the 3 thousands with the 2 hundreds (3,200).
- 8 goes into 32 four times $(3,200 \div 8 = 400)$
- 8 goes into 0 zero times (tens).
- 8 goes into 7 zero times, and leaves a remainder of 7.

Step 1 continued...

When dividing the ones, 4 goes into 7 one time. Multiply $1 \times 4 = 4$, write that four under the 7, and subract. This finds us the remainder of 3.

Check: $4 \times 61 + 3 = 247$

When dividing the ones, 4 goes into 9 two times. Multiply $2 \times 4 = 8$, write that eight under the 9, and subract. This finds us the remainder of 1.

Check: $4 \times 402 + 1 = 1,609$

Step 2—a remainder in the tens

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
t o 2 2)58	t o 2 2) <mark>5</mark> 8	t o 29 2)5 <mark>8</mark> -4↓
Two goes into 5 two times, or 5 tens ÷ 2 = 2 whole tens but there is a remainder!	To find it, multiply 2 × 2 = 4, write that 4 under the five, and subtract to find the remainder of 1 ten.	1 8 Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
2 <mark>9</mark> 2) 5 8	2 9 2) 5 8	2 9 2) 5 8
<u>- 4</u> 1 8	- 4 1 8 - 1 8 0	1 8 - 1 8 0
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract.	The division is over since there are no more digits in the dividend. The quotient is 29.



Step 2—a remainder in any of the place values

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
1 2)278	2)278 -20	1 8 2) 2 7 8 -2 1 0 7
Two goes into 2 one time, or 2 hundreds ÷ 2 = 1 hundred.	Multiply 1 × 2 = 2, write that 2 under the two, and subtract to find the remainder of zero.	Next, drop down the 7 of the tens next to the zero.
Divide.	Multiply & subtract.	Drop down the next digit.
h t o 1 3 2) 2 7 8 -2 0 7 Divide 2 into 7. Place 3 into the quotient.	$\begin{array}{c} h \text{ t o} \\ \hline 13 \\ \hline 2)278 \\ \hline -2 \\ \hline 07 \\ \hline -6 \\ \hline 1 \\ \hline \end{array}$ Multiply $3 \times 2 = 6$, write that 6 under the 7, and subtract to find the remainder of 1 ten.	h t o 13 2)278 -2 07 -6 18 Next, drop down the 8 of the ones next to the 1 leftover ten.
1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
13 <mark>9</mark> 2)278 -2 07 -6	139 2)278 -2 07 -6 18 -18	2)278 -2 07 -6 18 -18
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract to find the remainder of zero.	There are no more digits to drop down. The quotient is 139.